

1

INTRODUCTION

VISIT...



2

INTELLIGENT AGENTS

```
function TABLE-DRIVEN-AGENT(percept) returns an action
  persistent: percepts, a sequence, initially empty
            table, a table of actions, indexed by percept sequences, initially fully specified
  append percept to the end of percepts
  action  $\leftarrow$  LOOKUP(percepts, table)
  return action
```

Figure 2.3 The TABLE-DRIVEN-AGENT program is invoked for each new percept and returns an action each time. It retains the complete percept sequence in memory.

```
function REFLEX-VACUUM-AGENT([location,status]) returns an action
  if status = Dirty then return Suck
  else if location = A then return Right
  else if location = B then return Left
```

Figure 2.4 The agent program for a simple reflex agent in the two-state vacuum environment. This program implements the agent function tabulated in Figure ??.

```
function SIMPLE-REFLEX-AGENT(percept) returns an action
  persistent: rules, a set of condition-action rules
  state  $\leftarrow$  INTERPRET-INPUT(percept)
  rule  $\leftarrow$  RULE-MATCH(state, rules)
  action  $\leftarrow$  rule.ACTION
  return action
```

Figure 2.6 A simple reflex agent. It acts according to a rule whose condition matches the current state, as defined by the percept.

```
function MODEL-BASED-REFLEX-AGENT(percept) returns an action
  persistent: state, the agent's current conception of the world state
  model, a description of how the next state depends on current state and action
  rules, a set of condition-action rules
  action, the most recent action, initially none

  state  $\leftarrow$  UPDATE-STATE(state, action, percept, model)
  rule  $\leftarrow$  RULE-MATCH(state, rules)
  action  $\leftarrow$  rule.ACTION
  return action
```

Figure 2.8 A model-based reflex agent. It keeps track of the current state of the world, using an internal model. It then chooses an action in the same way as the reflex agent.

3

SOLVING PROBLEMS BY SEARCHING

```
function SIMPLE-PROBLEM-SOLVING-AGENT(percept) returns an action
    persistent: seq, an action sequence, initially empty
        state, some description of the current world state
        goal, a goal, initially null
        problem, a problem formulation

    state  $\leftarrow$  UPDATE-STATE(state, percept)
    if seq is empty then
        goal  $\leftarrow$  FORMULATE-GOAL(state)
        problem  $\leftarrow$  FORMULATE-PROBLEM(state, goal)
        seq  $\leftarrow$  SEARCH(problem)
        if seq = failure then return a null action
        action  $\leftarrow$  FIRST(seq)
        seq  $\leftarrow$  REST(seq)
    return action
```

Figure 3.1 A simple problem-solving agent. It first formulates a goal and a problem, searches for a sequence of actions that would solve the problem, and then executes the actions one at a time. When this is complete, it formulates another goal and starts over.

```

function TREE-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of problem
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    expand the chosen node, adding the resulting nodes to the frontier

function GRAPH-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of problem
  initialize the explored set to be empty
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    add the node to the explored set
    expand the chosen node, adding the resulting nodes to the frontier
    only if not in the frontier or explored set

```

Figure 3.7 An informal description of the general tree-search and graph-search algorithms. The parts of GRAPH-SEARCH marked in bold italic are the additions needed to handle repeated states.

```

function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure
  node  $\leftarrow$  a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  frontier  $\leftarrow$  a FIFO queue with node as the only element
  explored  $\leftarrow$  an empty set
  loop do
    if EMPTY?(frontier) then return failure
    node  $\leftarrow$  POP(frontier) /* chooses the shallowest node in frontier */
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child  $\leftarrow$  CHILD-NODE(problem, node, action)
      if child.STATE is not in explored or frontier then
        if problem.GOAL-TEST(child.STATE) then return SOLUTION(child)
        frontier  $\leftarrow$  INSERT(child, frontier)

```

Figure 3.11 Breadth-first search on a graph.

```

function UNIFORM-COST-SEARCH(problem) returns a solution, or failure
  node  $\leftarrow$  a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
  frontier  $\leftarrow$  a priority queue ordered by PATH-COST, with node as the only element
  explored  $\leftarrow$  an empty set
  loop do
    if EMPTY?(frontier) then return failure
    node  $\leftarrow$  POP(frontier) /* chooses the lowest-cost node in frontier */
    if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child  $\leftarrow$  CHILD-NODE(problem, node, action)
      if child.STATE is not in explored or frontier then
        frontier  $\leftarrow$  INSERT(child, frontier)
      else if child.STATE is in frontier with higher PATH-COST then
        replace that frontier node with child
  
```

Figure 3.13 Uniform-cost search on a graph. The algorithm is identical to the general graph search algorithm in Figure ??, except for the use of a priority queue and the addition of an extra check in case a shorter path to a frontier state is discovered. The data structure for *frontier* needs to support efficient membership testing, so it should combine the capabilities of a priority queue and a hash table.

```

function DEPTH-LIMITED-SEARCH(problem, limit) returns a solution, or failure/cutoff
  return RECURSIVE-DLS(MAKE-NODE(problem.INITIAL-STATE), problem, limit)

function RECURSIVE-DLS(node, problem, limit) returns a solution, or failure/cutoff
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  else if limit = 0 then return cutoff
  else
    cutoff_occurred?  $\leftarrow$  false
    for each action in problem.ACTIONS(node.STATE) do
      child  $\leftarrow$  CHILD-NODE(problem, node, action)
      result  $\leftarrow$  RECURSIVE-DLS(child, problem, limit - 1)
      if result = cutoff then cutoff_occurred?  $\leftarrow$  true
      else if result  $\neq$  failure then return result
      if cutoff_occurred? then return cutoff else return failure
  
```

Figure 3.16 A recursive implementation of depth-limited tree search.

```

function ITERATIVE-DEEPENING-SEARCH(problem) returns a solution, or failure
  for depth = 0 to  $\infty$  do
    result  $\leftarrow$  DEPTH-LIMITED-SEARCH(problem, depth)
    if result  $\neq$  cutoff then return result

```

Figure 3.17 The iterative deepening search algorithm, which repeatedly applies depth-limited search with increasing limits. It terminates when a solution is found or if the depth-limited search returns *failure*, meaning that no solution exists.

```

function RECURSIVE-BEST-FIRST-SEARCH(problem) returns a solution, or failure
  return RBFS(problem, MAKE-NODE(problem.INITIAL-STATE),  $\infty$ )

function RBFS(problem, node, f_limit) returns a solution, or failure and a new f-cost limit
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  successors  $\leftarrow$  []
  for each action in problem.ACTIONS(node.STATE) do
    add CHILD-NODE(problem, node, action) into successors
  if successors is empty then return failure,  $\infty$ 
  for each s in successors do /* update f with value from previous search, if any */
    s.f  $\leftarrow$  max(s.g + s.h, node.f)
  loop do
    best  $\leftarrow$  the lowest f-value node in successors
    if best.f  $>$  f_limit then return failure, best.f
    alternative  $\leftarrow$  the second-lowest f-value among successors
    result, best.f  $\leftarrow$  RBFS(problem, best, min(f_limit, alternative))
  if result  $\neq$  failure then return result

```

Figure 3.24 The algorithm for recursive best-first search.

4

BEYOND CLASSICAL SEARCH

```
function HILL-CLIMBING(problem) returns a state that is a local maximum
  current  $\leftarrow$  MAKE-NODE(problem.INITIAL-STATE)
  loop do
    neighbor  $\leftarrow$  a highest-valued successor of current
    if neighbor.VALUE  $\leq$  current.VALUE then return current.STATE
    current  $\leftarrow$  neighbor
```

Figure 4.2 The hill-climbing search algorithm, which is the most basic local search technique. At each step the current node is replaced by the best neighbor; in this version, that means the neighbor with the highest VALUE, but if a heuristic cost estimate h is used, we would find the neighbor with the lowest h .

```
function SIMULATED-ANNEALING(problem, schedule) returns a solution state
  inputs: problem, a problem
          schedule, a mapping from time to “temperature”
  current  $\leftarrow$  MAKE-NODE(problem.INITIAL-STATE)
  for  $t = 1$  to  $\infty$  do
     $T \leftarrow \text{schedule}(t)$ 
    if  $T = 0$  then return current
    next  $\leftarrow$  a randomly selected successor of current
     $\Delta E \leftarrow \text{next}.\text{VALUE} - \text{current}.\text{VALUE}$ 
    if  $\Delta E > 0$  then current  $\leftarrow$  next
    else current  $\leftarrow$  next only with probability  $e^{\Delta E/T}$ 
```

Figure 4.5 The simulated annealing algorithm, a version of stochastic hill climbing where some downhill moves are allowed. Downhill moves are accepted readily early in the annealing schedule and then less often as time goes on. The *schedule* input determines the value of the temperature T as a function of time.

```

function GENETIC-ALGORITHM(population, FITNESS-FN) returns an individual
  inputs: population, a set of individuals
    FITNESS-FN, a function that measures the fitness of an individual

  repeat
    new_population  $\leftarrow$  empty set
    for i = 1 to SIZE(population) do
      x  $\leftarrow$  RANDOM-SELECTION(population, FITNESS-FN)
      y  $\leftarrow$  RANDOM-SELECTION(population, FITNESS-FN)
      child  $\leftarrow$  REPRODUCE(x, y)
      if (small random probability) then child  $\leftarrow$  MUTATE(child)
      add child to new_population
    population  $\leftarrow$  new_population
  until some individual is fit enough, or enough time has elapsed
  return the best individual in population, according to FITNESS-FN

function REPRODUCE(x, y) returns an individual
  inputs: x, y, parent individuals

  n  $\leftarrow$  LENGTH(x); c  $\leftarrow$  random number from 1 to n
  return APPEND(SUBSTRING(x, 1, c), SUBSTRING(y, c + 1, n))

```

Figure 4.8 A genetic algorithm. The algorithm is the same as the one diagrammed in Figure ??, with one variation: in this more popular version, each mating of two parents produces only one offspring, not two.

```

function AND-OR-GRAFH-SEARCH(problem) returns a conditional plan, or failure
  OR-SEARCH(problem.INITIAL-STATE, problem, [])

function OR-SEARCH(state, problem, path) returns a conditional plan, or failure
  if problem.GOAL-TEST(state) then return the empty plan
  if state is on path then return failure
  for each action in problem.ACTIONS(state) do
    plan  $\leftarrow$  AND-SEARCH(RESULTS(state, action), problem, [state | path])
    if plan  $\neq$  failure then return [action | plan]
  return failure

function AND-SEARCH(states, problem, path) returns a conditional plan, or failure
  for each si in states do
    plani  $\leftarrow$  OR-SEARCH(si, problem, path)
    if plani = failure then return failure
  return [if s1 then plan1 else if s2 then plan2 else ... if sn-1 then plann-1 else plann]

```

Figure 4.11 An algorithm for searching AND-OR graphs generated by nondeterministic environments. It returns a conditional plan that reaches a goal state in all circumstances. (The notation [*x* | *l*] refers to the list formed by adding object *x* to the front of list *l*.)

```

function ONLINE-DFS-AGENT( $s'$ ) returns an action
  inputs:  $s'$ , a percept that identifies the current state
  persistent:  $result$ , a table indexed by state and action, initially empty
     $untried$ , a table that lists, for each state, the actions not yet tried
     $unbacktracked$ , a table that lists, for each state, the backtracks not yet tried
     $s, a$ , the previous state and action, initially null

  if GOAL-TEST( $s'$ ) then return stop
  if  $s'$  is a new state (not in  $untried$ ) then  $untried[s'] \leftarrow \text{ACTIONS}(s')$ 
  if  $s$  is not null then
     $result[s, a] \leftarrow s'$ 
    add  $s$  to the front of  $unbacktracked[s']$ 
  if  $untried[s']$  is empty then
    if  $unbacktracked[s']$  is empty then return stop
    else  $a \leftarrow$  an action  $b$  such that  $result[s', b] = \text{POP}(unbacktracked[s'])$ 
  else  $a \leftarrow \text{POP}(untried[s'])$ 
   $s \leftarrow s'$ 
  return  $a$ 

```

Figure 4.21 An online search agent that uses depth-first exploration. The agent is applicable only in state spaces in which every action can be “undone” by some other action.

```

function LRTA *-AGENT( $s'$ ) returns an action
  inputs:  $s'$ , a percept that identifies the current state
  persistent:  $result$ , a table, indexed by state and action, initially empty
     $H$ , a table of cost estimates indexed by state, initially empty
     $s, a$ , the previous state and action, initially null

  if GOAL-TEST( $s'$ ) then return stop
  if  $s'$  is a new state (not in  $H$ ) then  $H[s'] \leftarrow h(s')$ 
  if  $s$  is not null
     $result[s, a] \leftarrow s'$ 
     $H[s] \leftarrow \min_{b \in \text{ACTIONS}(s)} \text{LRTA}^*-\text{COST}(s, b, result[s, b], H)$ 
   $a \leftarrow$  an action  $b$  in  $\text{ACTIONS}(s')$  that minimizes  $\text{LRTA}^*-\text{COST}(s', b, result[s', b], H)$ 
   $s \leftarrow s'$ 
  return  $a$ 

function LRTA *-COST( $s, a, s', H$ ) returns a cost estimate
  if  $s'$  is undefined then return  $h(s)$ 
  else return  $c(s, a, s') + H[s']$ 

```

Figure 4.24 LRTA *-AGENT selects an action according to the values of neighboring states, which are updated as the agent moves about the state space.

5 ADVERSARIAL SEARCH

```
function MINIMAX-DECISION(state) returns an action
    return arg maxa ∈ ACTIONS(s) MIN-VALUE(RESULT(state, a))

function MAX-VALUE(state) returns a utility value
    if TERMINAL-TEST(state) then return UTILITY(state)
    v ← −∞
    for each a in ACTIONS(state) do
        v ← MAX(v, MIN-VALUE(RESULT(s, a)))
    return v

function MIN-VALUE(state) returns a utility value
    if TERMINAL-TEST(state) then return UTILITY(state)
    v ← ∞
    for each a in ACTIONS(state) do
        v ← MIN(v, MAX-VALUE(RESULT(s, a)))
    return v
```

Figure 5.3 An algorithm for calculating minimax decisions. It returns the action corresponding to the best possible move, that is, the move that leads to the outcome with the best utility, under the assumption that the opponent plays to minimize utility. The functions MAX-VALUE and MIN-VALUE go through the whole game tree, all the way to the leaves, to determine the backed-up value of a state. The notation $\operatorname{argmax}_{a \in S} f(a)$ computes the element *a* of set *S* that has the maximum value of *f(a)*.

```

function ALPHA-BETA-SEARCH(state) returns an action
  v  $\leftarrow$  MAX-VALUE(state,  $-\infty$ ,  $+\infty$ )
  return the action in ACTIONS(state) with value v

function MAX-VALUE(state,  $\alpha$ ,  $\beta$ ) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
  v  $\leftarrow -\infty$ 
  for each a in ACTIONS(state) do
    v  $\leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$ 
    if v  $\geq \beta$  then return v
     $\alpha \leftarrow \text{MAX}(\alpha, v)$ 
  return v

function MIN-VALUE(state,  $\alpha$ ,  $\beta$ ) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
  v  $\leftarrow +\infty$ 
  for each a in ACTIONS(state) do
    v  $\leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$ 
    if v  $\leq \alpha$  then return v
     $\beta \leftarrow \text{MIN}(\beta, v)$ 
  return v

```

Figure 5.7 The alpha–beta search algorithm. Notice that these routines are the same as the MINIMAX functions in Figure ??, except for the two lines in each of MIN-VALUE and MAX-VALUE that maintain α and β (and the bookkeeping to pass these parameters along).

6

CONSTRAINT SATISFACTION PROBLEMS

```
function AC-3(csp) returns false if an inconsistency is found and true otherwise
  inputs: csp, a binary CSP with components (X, D, C)
  local variables: queue, a queue of arcs, initially all the arcs in csp

  while queue is not empty do
    (Xi, Xj)  $\leftarrow$  REMOVE-FIRST(queue)
    if REVISE(csp, Xi, Xj) then
      if size of Di = 0 then return false
      for each Xk in Xi.NEIGHBORS - {Xj} do
        add (Xk, Xi) to queue
    return true



---


function REVISE(csp, Xi, Xj) returns true iff we revise the domain of Xi
  revised  $\leftarrow$  false
  for each x in Di do
    if no value y in Dj allows (x,y) to satisfy the constraint between Xi and Xj then
      delete x from Di
      revised  $\leftarrow$  true
  return revised
```

Figure 6.3 The arc-consistency algorithm AC-3. After applying AC-3, either every arc is arc-consistent, or some variable has an empty domain, indicating that the CSP cannot be solved. The name “AC-3” was used by the algorithm’s inventor (?) because it’s the third version developed in the paper.

```

function BACKTRACKING-SEARCH(csp) returns a solution, or failure
  return BACKTRACK({ }, csp)

function BACKTRACK(assignment, csp) returns a solution, or failure
  if assignment is complete then return assignment
  var  $\leftarrow$  SELECT-UNASSIGNED-VARIABLE(csp)
  for each value in ORDER-DOMAIN-VALUES(var, assignment, csp) do
    if value is consistent with assignment then
      add {var = value} to assignment
      inferences  $\leftarrow$  INFERENCE(csp, var, value)
      if inferences  $\neq$  failure then
        add inferences to assignment
        result  $\leftarrow$  BACKTRACK(assignment, csp)
        if result  $\neq$  failure then
          return result
        remove {var = value} and inferences from assignment
  return failure

```

Figure 6.5 A simple backtracking algorithm for constraint satisfaction problems. The algorithm is modeled on the recursive depth-first search of Chapter ???. By varying the functions SELECT-UNASSIGNED-VARIABLE and ORDER-DOMAIN-VALUES, we can implement the general-purpose heuristics discussed in the text. The function INFERENCE can optionally be used to impose arc-, path-, or *k*-consistency, as desired. If a value choice leads to failure (noticed either by INFERENCE or by BACKTRACK), then value assignments (including those made by INFERENCE) are removed from the current assignment and a new value is tried.

```

function MIN-CONFLICTS(csp, max_steps) returns a solution or failure
  inputs: csp, a constraint satisfaction problem
           max_steps, the number of steps allowed before giving up
  current  $\leftarrow$  an initial complete assignment for csp
  for i = 1 to max_steps do
    if current is a solution for csp then return current
    var  $\leftarrow$  a randomly chosen conflicted variable from csp.VARIABLES
    value  $\leftarrow$  the value v for var that minimizes CONFLICTS(var, v, current, csp)
    set var = value in current
  return failure

```

Figure 6.8 The MIN-CONFLICTS algorithm for solving CSPs by local search. The initial state may be chosen randomly or by a greedy assignment process that chooses a minimal-conflict value for each variable in turn. The CONFLICTS function counts the number of constraints violated by a particular value, given the rest of the current assignment.

```

function TREE-CSP-SOLVER(csp) returns a solution, or failure
  inputs: csp, a CSP with components X, D, C

  n  $\leftarrow$  number of variables in X
  assignment  $\leftarrow$  an empty assignment
  root  $\leftarrow$  any variable in X
  X  $\leftarrow$  TOPOLOGICALSORT(X, root)
  for j = n down to 2 do
    MAKE-ARC-CONSISTENT(PARENT(Xj), Xj)
    if it cannot be made consistent then return failure
  for i = 1 to n do
    assignment[Xi]  $\leftarrow$  any consistent value from Di
    if there is no consistent value then return failure
  return assignment

```

Figure 6.11 The TREE-CSP-SOLVER algorithm for solving tree-structured CSPs. If the CSP has a solution, we will find it in linear time; if not, we will detect a contradiction.

7 LOGICAL AGENTS

```
function KB-AGENT(percept) returns an action
  persistent: KB, a knowledge base
  t, a counter, initially 0, indicating time
  TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t))
  action  $\leftarrow$  ASK(KB, MAKE-ACTION-QUERY(t))
  TELL(KB, MAKE-ACTION-SENTENCE(action, t))
  t  $\leftarrow$  t + 1
  return action
```

Figure 7.1 A generic knowledge-based agent. Given a percept, the agent adds the percept to its knowledge base, asks the knowledge base for the best action, and tells the knowledge base that it has in fact taken that action.

```

function TT-ENTAILS?(KB,  $\alpha$ ) returns true or false
  inputs: KB, the knowledge base, a sentence in propositional logic
           $\alpha$ , the query, a sentence in propositional logic

  symbols  $\leftarrow$  a list of the proposition symbols in KB and  $\alpha$ 
  return TT-CHECK-ALL(KB,  $\alpha$ , symbols, { })

function TT-CHECK-ALL(KB,  $\alpha$ , symbols, model) returns true or false
  if EMPTY?(symbols) then
    if PL-TRUE?(KB, model) then return PL-TRUE?( $\alpha$ , model)
    else return true // when KB is false, always return true
  else do
    P  $\leftarrow$  FIRST(symbols)
    rest  $\leftarrow$  REST(symbols)
    return (TT-CHECK-ALL(KB,  $\alpha$ , rest, model  $\cup$  {P = true})
           and
           TT-CHECK-ALL(KB,  $\alpha$ , rest, model  $\cup$  {P = false}))

```

Figure 7.8 A truth-table enumeration algorithm for deciding propositional entailment. (TT stands for truth table.) PL-TRUE? returns *true* if a sentence holds within a model. The variable *model* represents a partial model—an assignment to some of the symbols. The keyword “**and**” is used here as a logical operation on its two arguments, returning *true* or *false*.

```

function PL-RESOLUTION(KB,  $\alpha$ ) returns true or false
  inputs: KB, the knowledge base, a sentence in propositional logic
           $\alpha$ , the query, a sentence in propositional logic

  clauses  $\leftarrow$  the set of clauses in the CNF representation of  $KB \wedge \neg\alpha$ 
  new  $\leftarrow$  { }
  loop do
    for each pair of clauses  $C_i, C_j$  in clauses do
      resolvents  $\leftarrow$  PL-RESOLVE( $C_i, C_j$ )
      if resolvents contains the empty clause then return true
      new  $\leftarrow$  new  $\cup$  resolvents
    if new  $\subseteq$  clauses then return false
    clauses  $\leftarrow$  clauses  $\cup$  new

```

Figure 7.9 A simple resolution algorithm for propositional logic. The function PL-RESOLVE returns the set of all possible clauses obtained by resolving its two inputs.

```

function PL-FC-ENTAILS?(KB, q) returns true or false
  inputs: KB, the knowledge base, a set of propositional definite clauses
           q, the query, a proposition symbol
  count  $\leftarrow$  a table, where count[c] is the number of symbols in c's premise
  inferred  $\leftarrow$  a table, where inferred[s] is initially false for all symbols
  agenda  $\leftarrow$  a queue of symbols, initially symbols known to be true in KB

  while agenda is not empty do
    p  $\leftarrow$  POP(agenda)
    if p = q then return true
    if inferred[p] = false then
      inferred[p]  $\leftarrow$  true
      for each clause c in KB where p is in c.PREMISE do
        decrement count[c]
        if count[c] = 0 then add c.CONCLUSION to agenda
  return false

```

Figure 7.12 The forward-chaining algorithm for propositional logic. The *agenda* keeps track of symbols known to be true but not yet “processed.” The *count* table keeps track of how many premises of each implication are as yet unknown. Whenever a new symbol *p* from the agenda is processed, the count is reduced by one for each implication in whose premise *p* appears (easily identified in constant time with appropriate indexing.) If a count reaches zero, all the premises of the implication are known, so its conclusion can be added to the agenda. Finally, we need to keep track of which symbols have been processed; a symbol that is already in the set of inferred symbols need not be added to the agenda again. This avoids redundant work and prevents loops caused by implications such as $P \Rightarrow Q$ and $Q \Rightarrow P$.

```

function DPLL-SATISFIABLE?(s) returns true or false
  inputs: s, a sentence in propositional logic

  clauses  $\leftarrow$  the set of clauses in the CNF representation of s
  symbols  $\leftarrow$  a list of the proposition symbols in s
  return DPLL(clauses, symbols, { })

function DPLL(clauses, symbols, model) returns true or false
  if every clause in clauses is true in model then return true
  if some clause in clauses is false in model then return false
  P, value  $\leftarrow$  FIND-PURE-SYMBOL(symbols, clauses, model)
  if P is non-null then return DPLL(clauses, symbols - P, model  $\cup$  {P=value})
  P, value  $\leftarrow$  FIND-UNIT-CLAUSE(clauses, model)
  if P is non-null then return DPLL(clauses, symbols - P, model  $\cup$  {P=value})
  P  $\leftarrow$  FIRST(symbols); rest  $\leftarrow$  REST(symbols)
  return DPLL(clauses, rest, model  $\cup$  {P=true}) or
         DPLL(clauses, rest, model  $\cup$  {P=false}))

```

Figure 7.14 The DPLL algorithm for checking satisfiability of a sentence in propositional logic. The ideas behind FIND-PURE-SYMBOL and FIND-UNIT-CLAUSE are described in the text; each returns a symbol (or null) and the truth value to assign to that symbol. Like TT-ENTAILS?, DPLL operates over partial models.

```

function WALKSAT(clauses, p, max_flips) returns a satisfying model or failure
  inputs: clauses, a set of clauses in propositional logic
          p, the probability of choosing to do a “random walk” move, typically around 0.5
          max_flips, number of flips allowed before giving up

  model  $\leftarrow$  a random assignment of true/false to the symbols in clauses
  for i = 1 to max_flips do
    if model satisfies clauses then return model
    clause  $\leftarrow$  a randomly selected clause from clauses that is false in model
    with probability p flip the value in model of a randomly selected symbol from clause
    else flip whichever symbol in clause maximizes the number of satisfied clauses
  return failure

```

Figure 7.15 The WALKSAT algorithm for checking satisfiability by randomly flipping the values of variables. Many versions of the algorithm exist.

```

function HYBRID-WUMPUS-AGENT(percept) returns an action
  inputs: percept, a list, [stench,breeze,glitter,bump,scream]
  persistent: KB, a knowledge base, initially the atemporal “wumpus physics”
    t, a counter, initially 0, indicating time
    plan, an action sequence, initially empty

  TELL(KB, MAKE-PERCEPNT-SENTENCE(percept, t))
  TELL the KB the temporal “physics” sentences for time t
  safe  $\leftarrow \{[x, y] : \text{ASK}(KB, OK_{x,y}^t) = \text{true}\}$ 
  if ASK(KB, Glittert) = true then
    plan  $\leftarrow [\text{Grab}] + \text{PLAN-ROUTE}(\text{current}, \{[1,1]\}, \text{safe}) + [\text{Climb}]$ 
  if plan is empty then
    unvisited  $\leftarrow \{[x, y] : \text{ASK}(KB, L_{x,y}^{t'}) = \text{false} \text{ for all } t' \leq t\}$ 
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \text{unvisited} \cap \text{safe}, \text{safe})$ 
  if plan is empty and ASK(KB, HaveArrowt) = true then
    possible_wumpus  $\leftarrow \{[x, y] : \text{ASK}(KB, \neg W_{x,y}) = \text{false}\}$ 
    plan  $\leftarrow \text{PLAN-SHOT}(\text{current}, \text{possible\_wumpus}, \text{safe})$ 
  if plan is empty then // no choice but to take a risk
    not_unsafe  $\leftarrow \{[x, y] : \text{ASK}(KB, \neg OK_{x,y}^t) = \text{false}\}$ 
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \text{unvisited} \cap \text{not\_unsafe}, \text{safe})$ 
  if plan is empty then
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \{[1, 1]\}, \text{safe}) + [\text{Climb}]$ 
  action  $\leftarrow \text{POP}(\text{plan})$ 
  TELL(KB, MAKE-ACTION-SENTENCE(action, t))
  t  $\leftarrow t + 1$ 
  return action

function PLAN-ROUTE(current,goals,allowed) returns an action sequence
  inputs: current, the agent’s current position
    goals, a set of squares; try to plan a route to one of them
    allowed, a set of squares that can form part of the route

  problem  $\leftarrow \text{ROUTE-PROBLEM}(\text{current}, \text{goals}, \text{allowed})$ 
  return A*-GRAPH-SEARCH(problem)

```

Figure 7.17 A hybrid agent program for the wumpus world. It uses a propositional knowledge base to infer the state of the world, and a combination of problem-solving search and domain-specific code to decide what actions to take.

```

function SATPLAN(init, transition, goal,  $T_{\max}$ ) returns solution or failure
  inputs: init, transition, goal, constitute a description of the problem
     $T_{\max}$ , an upper limit for plan length

  for  $t = 0$  to  $T_{\max}$  do
     $cnf \leftarrow \text{TRANSLATE-TO-SAT}(\textit{init}, \textit{transition}, \textit{goal}, t)$ 
     $model \leftarrow \text{SAT-SOLVER}(cnf)$ 
    if model is not null then
      return EXTRACT-SOLUTION(model)
  return failure

```

Figure 7.19 The SATPLAN algorithm. The planning problem is translated into a CNF sentence in which the goal is asserted to hold at a fixed time step t and axioms are included for each time step up to t . If the satisfiability algorithm finds a model, then a plan is extracted by looking at those proposition symbols that refer to actions and are assigned *true* in the model. If no model exists, then the process is repeated with the goal moved one step later.

8

FIRST-ORDER LOGIC

9

INFERENCE IN FIRST-ORDER LOGIC

```
function UNIFY( $x, y, \theta$ ) returns a substitution to make  $x$  and  $y$  identical
    inputs:  $x$ , a variable, constant, list, or compound expression
             $y$ , a variable, constant, list, or compound expression
             $\theta$ , the substitution built up so far (optional, defaults to empty)

    if  $\theta = \text{failure}$  then return failure
    else if  $x = y$  then return  $\theta$ 
    else if VARIABLE?( $x$ ) then return UNIFY-VAR( $x, y, \theta$ )
    else if VARIABLE?( $y$ ) then return UNIFY-VAR( $y, x, \theta$ )
    else if COMPOUND?( $x$ ) and COMPOUND?( $y$ ) then
        return UNIFY( $x.\text{ARGS}, y.\text{ARGS}, \text{UNIFY}(x.\text{OP}, y.\text{OP}, \theta)$ )
    else if LIST?( $x$ ) and LIST?( $y$ ) then
        return UNIFY( $x.\text{REST}, y.\text{REST}, \text{UNIFY}(x.\text{FIRST}, y.\text{FIRST}, \theta)$ )
    else return failure

function UNIFY-VAR( $var, x, \theta$ ) returns a substitution
    if  $\{var/val\} \in \theta$  then return UNIFY( $val, x, \theta$ )
    else if  $\{x/val\} \in \theta$  then return UNIFY( $var, val, \theta$ )
    else if OCCUR-CHECK?( $var, x$ ) then return failure
    else return add  $\{var/x\}$  to  $\theta$ 
```

Figure 9.1 The unification algorithm. The algorithm works by comparing the structures of the inputs, element by element. The substitution θ that is the argument to UNIFY is built up along the way and is used to make sure that later comparisons are consistent with bindings that were established earlier. In a compound expression such as $F(A, B)$, the OP field picks out the function symbol F and the ARGS field picks out the argument list (A, B) .

```

function FOL-FC-ASK( $KB, \alpha$ ) returns a substitution or false
  inputs:  $KB$ , the knowledge base, a set of first-order definite clauses
     $\alpha$ , the query, an atomic sentence
  local variables:  $new$ , the new sentences inferred on each iteration

  repeat until  $new$  is empty
     $new \leftarrow \{ \}$ 
    for each  $rule$  in  $KB$  do
       $(p_1 \wedge \dots \wedge p_n \Rightarrow q) \leftarrow \text{STANDARDIZE-VARIABLES}(rule)$ 
      for each  $\theta$  such that  $\text{SUBST}(\theta, p_1 \wedge \dots \wedge p_n) = \text{SUBST}(\theta, p'_1 \wedge \dots \wedge p'_n)$ 
        for some  $p'_1, \dots, p'_n$  in  $KB$ 
         $q' \leftarrow \text{SUBST}(\theta, q)$ 
        if  $q'$  does not unify with some sentence already in  $KB$  or  $new$  then
          add  $q'$  to  $new$ 
           $\phi \leftarrow \text{UNIFY}(q', \alpha)$ 
          if  $\phi$  is not fail then return  $\phi$ 
        add  $new$  to  $KB$ 
    return false

```

Figure 9.3 A conceptually straightforward, but very inefficient, forward-chaining algorithm. On each iteration, it adds to KB all the atomic sentences that can be inferred in one step from the implication sentences and the atomic sentences already in KB . The function STANDARDIZE-VARIABLES replaces all variables in its arguments with new ones that have not been used before.

```

function FOL-BC-ASK( $KB, query$ ) returns a generator of substitutions
  return FOL-BC-OR( $KB, query, \{ \}$ )

generator FOL-BC-OR( $KB, goal, \theta$ ) yields a substitution
  for each rule  $(lhs \Rightarrow rhs)$  in  $\text{FETCH-RULES-FOR-GOAL}(KB, goal)$  do
     $(lhs, rhs) \leftarrow \text{STANDARDIZE-VARIABLES}((lhs, rhs))$ 
    for each  $\theta'$  in  $\text{FOL-BC-AND}(KB, lhs, \text{UNIFY}(rhs, goal, \theta))$  do
      yield  $\theta'$ 

generator FOL-BC-AND( $KB, goals, \theta$ ) yields a substitution
  if  $\theta = \text{failure}$  then return
  else if  $\text{LENGTH}(goals) = 0$  then yield  $\theta$ 
  else do
     $first, rest \leftarrow \text{FIRST}(goals), \text{REST}(goals)$ 
    for each  $\theta'$  in  $\text{FOL-BC-OR}(KB, \text{SUBST}(\theta, first), \theta)$  do
      for each  $\theta''$  in  $\text{FOL-BC-AND}(KB, rest, \theta')$  do
        yield  $\theta''$ 

```

Figure 9.6 A simple backward-chaining algorithm for first-order knowledge bases.

```
procedure APPEND( $ax, y, az, continuation$ )
     $trail \leftarrow \text{GLOBAL-TRAIL-POINTER}$ 
    if  $ax = []$  and UNIFY( $y, az$ ) then CALL( $continuation$ )
    RESET-TRAIL( $trail$ )
     $a, x, z \leftarrow \text{NEW-VARIABLE}(), \text{NEW-VARIABLE}(), \text{NEW-VARIABLE}()$ 
    if UNIFY( $ax, [a \mid x]$ ) and UNIFY( $az, [a \mid z]$ ) then APPEND( $x, y, z, continuation$ )
```

Figure 9.8 Pseudocode representing the result of compiling the Append predicate. The function NEW-VARIABLE returns a new variable, distinct from all other variables used so far. The procedure CALL($continuation$) continues execution with the specified continuation.

10 CLASSICAL PLANNING

```

Init(At(C1, SFO) ∧ At(C2, JFK) ∧ At(P1, SFO) ∧ At(P2, JFK)
     ∧ Cargo(C1) ∧ Cargo(C2) ∧ Plane(P1) ∧ Plane(P2)
     ∧ Airport(JFK) ∧ Airport(SFO))
Goal(At(C1, JFK) ∧ At(C2, SFO))
Action(Load(c, p, a),
    PRECOND: At(c, a) ∧ At(p, a) ∧ Cargo(c) ∧ Plane(p) ∧ Airport(a)
    EFFECT: ¬ At(c, a) ∧ In(c, p))
Action(Unload(c, p, a),
    PRECOND: In(c, p) ∧ At(p, a) ∧ Cargo(c) ∧ Plane(p) ∧ Airport(a)
    EFFECT: At(c, a) ∧ ¬ In(c, p))
Action(Fly(p, from, to),
    PRECOND: At(p, from) ∧ Plane(p) ∧ Airport(from) ∧ Airport(to)
    EFFECT: ¬ At(p, from) ∧ At(p, to))

```

Figure 10.1 A PDDL description of an air cargo transportation planning problem.

```

Init(Tire(Flat) ∧ Tire(Spare) ∧ At(Flat, Axle) ∧ At(Spare, Trunk))
Goal(At(Spare, Axle))
Action(Remove(obj, loc),
    PRECOND: At(obj, loc)
    EFFECT: ¬ At(obj, loc) ∧ At(obj, Ground))
Action(PutOn(t, Axle),
    PRECOND: Tire(t) ∧ At(t, Ground) ∧ ¬ At(Flat, Axle)
    EFFECT: ¬ At(t, Ground) ∧ At(t, Axle))
Action(LeaveOvernight,
    PRECOND:
    EFFECT: ¬ At(Spare, Ground) ∧ ¬ At(Spare, Axle) ∧ ¬ At(Spare, Trunk)
           ∧ ¬ At(Flat, Ground) ∧ ¬ At(Flat, Axle) ∧ ¬ At(Flat, Trunk))

```

Figure 10.2 The simple spare tire problem.

```

Init(On(A, Table) ∧ On(B, Table) ∧ On(C, A)
     ∧ Block(A) ∧ Block(B) ∧ Block(C) ∧ Clear(B) ∧ Clear(C))
Goal(On(A, B) ∧ On(B, C))
Action(Move(b, x, y),
       PRECOND: On(b, x) ∧ Clear(b) ∧ Clear(y) ∧ Block(b) ∧ Block(y) ∧
                  (b≠x) ∧ (b≠y) ∧ (x≠y),
       EFFECT: On(b, y) ∧ Clear(x) ∧ ¬On(b, x) ∧ ¬Clear(y))
Action(MoveToTable(b, x),
       PRECOND: On(b, x) ∧ Clear(b) ∧ Block(b) ∧ (b≠x),
       EFFECT: On(b, Table) ∧ Clear(x) ∧ ¬On(b, x))

```

Figure 10.3 A planning problem in the blocks world: building a three-block tower. One solution is the sequence [MoveToTable(C, A), Move(B, Table, C), Move(A, Table, B)].

```

Init(Have(Cake))
Goal(Have(Cake) ∧ Eaten(Cake))
Action(Eat(Cake)
      PRECOND: Have(Cake)
      EFFECT: ¬Have(Cake) ∧ Eaten(Cake))
Action(Bake(Cake)
      PRECOND: ¬Have(Cake)
      EFFECT: Have(Cake))

```

Figure 10.7 The “have cake and eat cake too” problem.

```

function GRAPHPLAN(problem) returns solution or failure
  graph ← INITIAL-PLANNING-GRAFH(problem)
  goals ← CONJUNCTS(problem.GOAL)
  nogoods ← an empty hash table
  for tl = 0 to  $\infty$  do
    if goals all non-mutex in St of graph then
      solution ← EXTRACT-SOLUTION(graph, goals, NUMLEVELS(graph), nogoods)
      if solution ≠ failure then return solution
    if graph and nogoods have both leveled off then return failure
    graph ← EXPAND-GRAFH(graph, problem)

```

Figure 10.9 The GRAPHPLAN algorithm. GRAPHPLAN calls EXPAND-GRAFH to add a level until either a solution is found by EXTRACT-SOLUTION, or no solution is possible.

11 PLANNING AND ACTING IN THE REAL WORLD

```
Jobs({AddEngine1 < AddWheels1 < Inspect1},  
     {AddEngine2 < AddWheels2 < Inspect2})  
  
Resources(EngineHoists(1), WheelStations(1), Inspectors(2), LugNuts(500))  
  
Action(AddEngine1, DURATION:30,  
       USE:EngineHoists(1))  
Action(AddEngine2, DURATION:60,  
       USE:EngineHoists(1))  
Action(AddWheels1, DURATION:30,  
      CONSUME:LugNuts(20), USE:WheelStations(1))  
Action(AddWheels2, DURATION:15,  
      CONSUME:LugNuts(20), USE:WheelStations(1))  
Action(Inspecti, DURATION:10,  
      USE:Inspectors(1))
```

Figure 11.1 A job-shop scheduling problem for assembling two cars, with resource constraints. The notation $A \prec B$ means that action A must precede action B .

```

Refinement(Go(Home, SFO),
  STEPS: [Drive(Home, SFOLongTermParking),
            Shuttle(SFOLongTermParking, SFO)] )
Refinement(Go(Home, SFO),
  STEPS: [Taxi(Home, SFO)] )

Refinement(Navigate([a, b], [x, y])),
  PRECOND: a = x  $\wedge$  b = y
  STEPS: []
Refinement(Navigate([a, b], [x, y])),
  PRECOND: Connected([a, b], [a - 1, b])
  STEPS: [Left, Navigate([a - 1, b], [x, y])] )
Refinement(Navigate([a, b], [x, y])),
  PRECOND: Connected([a, b], [a + 1, b])
  STEPS: [Right, Navigate([a + 1, b], [x, y])] )
...

```

Figure 11.4 Definitions of possible refinements for two high-level actions: going to San Francisco airport and navigating in the vacuum world. In the latter case, note the recursive nature of the refinements and the use of preconditions.

```

function HIERARCHICAL-SEARCH(problem, hierarchy) returns a solution, or failure
  frontier  $\leftarrow$  a FIFO queue with [Act] as the only element
  loop do
    if EMPTY?(frontier) then return failure
    plan  $\leftarrow$  POP(frontier) /* chooses the shallowest plan in frontier */
    hla  $\leftarrow$  the first HLA in plan, or null if none
    prefix, suffix  $\leftarrow$  the action subsequences before and after hla in plan
    outcome  $\leftarrow$  RESULT(problem.INITIAL-STATE, prefix)
    if hla is null then /* so plan is primitive and outcome is its result */
      if outcome satisfies problem.GOAL then return plan
    else for each sequence in REFINEMENTS(hla, outcome, hierarchy) do
      frontier  $\leftarrow$  INSERT(APPEND(prefix, sequence, suffix), frontier)

```

Figure 11.5 A breadth-first implementation of hierarchical forward planning search. The initial plan supplied to the algorithm is [*Act*]. The REFINEMENTS function returns a set of action sequences, one for each refinement of the HLA whose preconditions are satisfied by the specified state, *outcome*.

```

function ANGELIC-SEARCH(problem, hierarchy, initialPlan) returns solution or fail
  frontier  $\leftarrow$  a FIFO queue with initialPlan as the only element
  loop do
    if EMPTY?(frontier) then return fail
    plan  $\leftarrow$  POP(frontier) /* chooses the shallowest node in frontier */
    if REACH+(problem.INITIAL-STATE, plan) intersects problem.GOAL then
      if plan is primitive then return plan /* REACH+ is exact for primitive plans */
      guaranteed  $\leftarrow$  REACH-(problem.INITIAL-STATE, plan)  $\cap$  problem.GOAL
      if guaranteed $\neq\{\}$  and MAKING-PROGRESS(plan, initialPlan) then
        finalState  $\leftarrow$  any element of guaranteed
        return DECOMPOSE(hierarchy, problem.INITIAL-STATE, plan, finalState)
      hla  $\leftarrow$  some HLA in plan
      prefix, suffix  $\leftarrow$  the action subsequences before and after hla in plan
      for each sequence in REFINEMENTS(hla, outcome, hierarchy) do
        frontier  $\leftarrow$  INSERT(APPEND(prefix, sequence, suffix), frontier)
    function DECOMPOSE(hierarchy, so, plan, sf) returns a solution
      solution  $\leftarrow$  an empty plan
      while plan is not empty do
        action  $\leftarrow$  REMOVE-LAST(plan)
        si  $\leftarrow$  a state in REACH-(s0, plan) such that sf  $\in$  REACH-(si, action)
        problem  $\leftarrow$  a problem with INITIAL-STATE = si and GOAL = sf
        solution  $\leftarrow$  APPEND(ANGELIC-SEARCH(problem, hierarchy, action), solution)
        sf  $\leftarrow$  si
      return solution

```

Figure 11.8 A hierarchical planning algorithm that uses angelic semantics to identify and commit to high-level plans that work while avoiding high-level plans that don't. The predicate MAKING-PROGRESS checks to make sure that we aren't stuck in an infinite regression of refinements. At top level, call ANGELIC-SEARCH with [Act] as the *initialPlan*.

```

Actors(A, B)
Init(At(A, LeftBaseline)  $\wedge$  At(B, RightNet)  $\wedge$ 
Approaching(Ball, RightBaseline))  $\wedge$  Partner(A, B)  $\wedge$  Partner(B, A)
Goal(Returned(Ball)  $\wedge$  (At(a, RightNet)  $\vee$  At(a, LeftNet)))
Action(Hit(actor, Ball),
  PRECOND:Approaching(Ball, loc)  $\wedge$  At(actor, loc)
  EFFECT:Returned(Ball))
Action(Go(actor, to),
  PRECOND:At(actor, loc)  $\wedge$  to  $\neq$  loc,
  EFFECT:At(actor, to)  $\wedge$   $\neg$  At(actor, loc))

```

Figure 11.10 The doubles tennis problem. Two actors *A* and *B* are playing together and can be in one of four locations: *LeftBaseline*, *RightBaseline*, *LeftNet*, and *RightNet*. The ball can be returned only if a player is in the right place. Note that each action must include the actor as an argument.

12 KNOWLEDGE REPRESENTATION

13 QUANTIFYING UNCERTAINTY

```
function DT-AGENT(percept) returns an action
    persistent: belief-state, probabilistic beliefs about the current state of the world
                action, the agent's action

    update belief-state based on action and percept
    calculate outcome probabilities for actions,
        given action descriptions and current belief-state
    select action with highest expected utility
        given probabilities of outcomes and utility information
    return action
```

Figure 13.1 A decision-theoretic agent that selects rational actions.

14 PROBABILISTIC REASONING

```

function ENUMERATION-ASK( $X, \mathbf{e}, bn$ ) returns a distribution over  $X$ 
  inputs:  $X$ , the query variable
   $\mathbf{e}$ , observed values for variables  $\mathbf{E}$ 
   $bn$ , a Bayes net with variables  $\{X\} \cup \mathbf{E} \cup \mathbf{Y}$  /*  $\mathbf{Y} = \text{hidden variables}$  */

   $\mathbf{Q}(X) \leftarrow$  a distribution over  $X$ , initially empty
  for each value  $x_i$  of  $X$  do
     $\mathbf{Q}(x_i) \leftarrow$  ENUMERATE-ALL( $bn.\text{VARS}, \mathbf{e}_{x_i}$ )
      where  $\mathbf{e}_{x_i}$  is  $\mathbf{e}$  extended with  $X = x_i$ 
  return NORMALIZE( $\mathbf{Q}(X)$ )

function ENUMERATE-ALL( $vars, \mathbf{e}$ ) returns a real number
  if EMPTY?( $vars$ ) then return 1.0
   $Y \leftarrow \text{FIRST}(vars)$ 
  if  $Y$  has value  $y$  in  $\mathbf{e}$ 
    then return  $P(y | parents(Y)) \times$  ENUMERATE-ALL( $\text{REST}(vars), \mathbf{e}$ )
    else return  $\sum_y P(y | parents(Y)) \times$  ENUMERATE-ALL( $\text{REST}(vars), \mathbf{e}_y$ )
      where  $\mathbf{e}_y$  is  $\mathbf{e}$  extended with  $Y = y$ 

```

Figure 14.9 The enumeration algorithm for answering queries on Bayesian networks.

```

function ELIMINATION-ASK( $X, \mathbf{e}, bn$ ) returns a distribution over  $X$ 
  inputs:  $X$ , the query variable
   $\mathbf{e}$ , observed values for variables  $\mathbf{E}$ 
   $bn$ , a Bayesian network specifying joint distribution  $\mathbf{P}(X_1, \dots, X_n)$ 

   $factors \leftarrow []$ 
  for each  $var$  in ORDER( $bn.\text{VARS}$ ) do
     $factors \leftarrow [\text{MAKE-FACTOR}(var, \mathbf{e}) | factors]$ 
    if  $var$  is a hidden variable then  $factors \leftarrow \text{SUM-OUT}(var, factors)$ 
  return NORMALIZE(POINTWISE-PRODUCT( $factors$ ))

```

Figure 14.10 The variable elimination algorithm for inference in Bayesian networks.

```

function PRIOR-SAMPLE(bn) returns an event sampled from the prior specified by bn
  inputs: bn, a Bayesian network specifying joint distribution  $\mathbf{P}(X_1, \dots, X_n)$ 
    x  $\leftarrow$  an event with n elements
    foreach variable  $X_i$  in  $X_1, \dots, X_n$  do
       $x[i] \leftarrow$  a random sample from  $\mathbf{P}(X_i | \text{parents}(X_i))$ 
    return x

```

Figure 14.12 A sampling algorithm that generates events from a Bayesian network. Each variable is sampled according to the conditional distribution given the values already sampled for the variable's parents.

```

function REJECTION-SAMPLING(X, e, bn, N) returns an estimate of  $\mathbf{P}(X|\mathbf{e})$ 
  inputs: X, the query variable
    e, observed values for variables E
    bn, a Bayesian network
    N, the total number of samples to be generated
  local variables: N, a vector of counts for each value of X, initially zero
    for j = 1 to N do
      x  $\leftarrow$  PRIOR-SAMPLE(bn)
      if x is consistent with e then
         $\mathbf{N}[x] \leftarrow \mathbf{N}[x]+1$  where x is the value of X in x
    return NORMALIZE(N)

```

Figure 14.13 The rejection-sampling algorithm for answering queries given evidence in a Bayesian network.

```

function LIKELIHOOD-WEIGHTING( $X, \mathbf{e}, bn, N$ ) returns an estimate of  $\mathbf{P}(X|\mathbf{e})$ 
  inputs:  $X$ , the query variable
     $\mathbf{e}$ , observed values for variables  $\mathbf{E}$ 
     $bn$ , a Bayesian network specifying joint distribution  $\mathbf{P}(X_1, \dots, X_n)$ 
     $N$ , the total number of samples to be generated
  local variables:  $\mathbf{W}$ , a vector of weighted counts for each value of  $X$ , initially zero

  for  $j = 1$  to  $N$  do
     $\mathbf{x}, w \leftarrow \text{WEIGHTED-SAMPLE}(bn, \mathbf{e})$ 
     $\mathbf{W}[x] \leftarrow \mathbf{W}[x] + w$  where  $x$  is the value of  $X$  in  $\mathbf{x}$ 
  return NORMALIZE( $\mathbf{W}$ )

```

```

function WEIGHTED-SAMPLE( $bn, \mathbf{e}$ ) returns an event and a weight
   $w \leftarrow 1; \mathbf{x} \leftarrow$  an event with  $n$  elements initialized from  $\mathbf{e}$ 
  foreach variable  $X_i$  in  $X_1, \dots, X_n$  do
    if  $X_i$  is an evidence variable with value  $x_i$  in  $\mathbf{e}$ 
      then  $w \leftarrow w \times P(X_i = x_i | \text{parents}(X_i))$ 
      else  $\mathbf{x}[i] \leftarrow$  a random sample from  $\mathbf{P}(X_i | \text{parents}(X_i))$ 
  return  $\mathbf{x}, w$ 

```

Figure 14.14 The likelihood-weighting algorithm for inference in Bayesian networks. In WEIGHTED-SAMPLE, each nonevidence variable is sampled according to the conditional distribution given the values already sampled for the variable's parents, while a weight is accumulated based on the likelihood for each evidence variable.

```

function GIBBS-ASK( $X, \mathbf{e}, bn, N$ ) returns an estimate of  $\mathbf{P}(X|\mathbf{e})$ 
  local variables:  $\mathbf{N}$ , a vector of counts for each value of  $X$ , initially zero
     $\mathbf{Z}$ , the nonevidence variables in  $bn$ 
     $\mathbf{x}$ , the current state of the network, initially copied from  $\mathbf{e}$ 

  initialize  $\mathbf{x}$  with random values for the variables in  $\mathbf{Z}$ 
  for  $j = 1$  to  $N$  do
    for each  $Z_i$  in  $\mathbf{Z}$  do
      set the value of  $Z_i$  in  $\mathbf{x}$  by sampling from  $\mathbf{P}(Z_i | mb(Z_i))$ 
       $\mathbf{N}[x] \leftarrow \mathbf{N}[x] + 1$  where  $x$  is the value of  $X$  in  $\mathbf{x}$ 
  return NORMALIZE( $\mathbf{N}$ )

```

Figure 14.15 The Gibbs sampling algorithm for approximate inference in Bayesian networks; this version cycles through the variables, but choosing variables at random also works.

15 PROBABILISTIC REASONING OVER TIME

```
function FORWARD-BACKWARD(ev, prior) returns a vector of probability distributions
  inputs: ev, a vector of evidence values for steps 1, . . . , t
          prior, the prior distribution on the initial state, P(X0)
  local variables: fv, a vector of forward messages for steps 0, . . . , t
                  b, a representation of the backward message, initially all 1s
                  sv, a vector of smoothed estimates for steps 1, . . . , t

  fv[0] ← prior
  for i = 1 to t do
    fv[i] ← FORWARD(fv[i - 1], ev[i])
  for i = t downto 1 do
    sv[i] ← NORMALIZE(fv[i] × b)
    b ← BACKWARD(b, ev[i])
  return sv
```

Figure 15.4 The forward–backward algorithm for smoothing: computing posterior probabilities of a sequence of states given a sequence of observations. The FORWARD and BACKWARD operators are defined by Equations (??) and (??), respectively.

```

function FIXED-LAG-SMOOTHING( $e_t, hmm, d$ ) returns a distribution over  $\mathbf{X}_{t-d}$ 
  inputs:  $e_t$ , the current evidence for time step  $t$ 
            $hmm$ , a hidden Markov model with  $S \times S$  transition matrix  $\mathbf{T}$ 
            $d$ , the length of the lag for smoothing
  persistent:  $t$ , the current time, initially 1
   $\mathbf{f}$ , the forward message  $\mathbf{P}(X_t|e_{1:t})$ , initially  $hmm.\text{PRIOR}$ 
   $\mathbf{B}$ , the  $d$ -step backward transformation matrix, initially the identity matrix
   $e_{t-d:t}$ , double-ended list of evidence from  $t-d$  to  $t$ , initially empty
  local variables:  $\mathbf{O}_{t-d}, \mathbf{O}_t$ , diagonal matrices containing the sensor model information

  add  $e_t$  to the end of  $e_{t-d:t}$ 
   $\mathbf{O}_t \leftarrow$  diagonal matrix containing  $\mathbf{P}(e_t|X_t)$ 
  if  $t > d$  then
     $\mathbf{f} \leftarrow \text{FORWARD}(\mathbf{f}, e_t)$ 
    remove  $e_{t-d-1}$  from the beginning of  $e_{t-d:t}$ 
     $\mathbf{O}_{t-d} \leftarrow$  diagonal matrix containing  $\mathbf{P}(e_{t-d}|X_{t-d})$ 
     $\mathbf{B} \leftarrow \mathbf{O}_{t-d}^{-1} \mathbf{T}^{-1} \mathbf{B} \mathbf{O}_t$ 
  else  $\mathbf{B} \leftarrow \mathbf{B} \mathbf{O}_t$ 
   $t \leftarrow t + 1$ 
  if  $t > d$  then return NORMALIZE( $\mathbf{f} \times \mathbf{B} \mathbf{1}$ ) else return null

```

Figure 15.6 An algorithm for smoothing with a fixed time lag of d steps, implemented as an online algorithm that outputs the new smoothed estimate given the observation for a new time step. Notice that the final output NORMALIZE($\mathbf{f} \times \mathbf{B} \mathbf{1}$) is just $\alpha \mathbf{f} \times \mathbf{b}$, by Equation (??).

```

function PARTICLE-FILTERING( $\mathbf{e}, N, dbn$ ) returns a set of samples for the next time step
  inputs:  $\mathbf{e}$ , the new incoming evidence
            $N$ , the number of samples to be maintained
            $dbn$ , a DBN with prior  $\mathbf{P}(\mathbf{X}_0)$ , transition model  $\mathbf{P}(\mathbf{X}_1|\mathbf{X}_0)$ , sensor model  $\mathbf{P}(\mathbf{E}_1|\mathbf{X}_1)$ 
  persistent:  $S$ , a vector of samples of size  $N$ , initially generated from  $\mathbf{P}(\mathbf{X}_0)$ 
  local variables:  $W$ , a vector of weights of size  $N$ 

  for  $i = 1$  to  $N$  do
     $S[i] \leftarrow$  sample from  $\mathbf{P}(\mathbf{X}_1 | \mathbf{X}_0 = S[i])$  /* step 1 */
     $W[i] \leftarrow \mathbf{P}(\mathbf{e} | \mathbf{X}_1 = S[i])$  /* step 2 */
     $S \leftarrow \text{WEIGHTED-SAMPLE-WITH-REPLACEMENT}(N, S, W)$  /* step 3 */
  return  $S$ 

```

Figure 15.17 The particle filtering algorithm implemented as a recursive update operation with state (the set of samples). Each of the sampling operations involves sampling the relevant slice variables in topological order, much as in PRIOR-SAMPLE. The WEIGHTED-SAMPLE-WITH-REPLACEMENT operation can be implemented to run in $O(N)$ expected time. The step numbers refer to the description in the text.

16 MAKING SIMPLE DECISIONS

```
function INFORMATION-GATHERING-AGENT(percept) returns an action
  persistent: D, a decision network
```

```
    integrate percept into D
    j  $\leftarrow$  the value that maximizes  $VPI(E_j) / Cost(E_j)$ 
    if  $VPI(E_j) > Cost(E_j)$ 
      return REQUEST(Ej)
    else return the best action from D
```

Figure 16.9 Design of a simple information-gathering agent. The agent works by repeatedly selecting the observation with the highest information value, until the cost of the next observation is greater than its expected benefit.

17 MAKING COMPLEX DECISIONS

```
function VALUE-ITERATION( $mdp, \epsilon$ ) returns a utility function
  inputs:  $mdp$ , an MDP with states  $S$ , actions  $A(s)$ , transition model  $P(s' | s, a)$ ,
          rewards  $R(s)$ , discount  $\gamma$ 
           $\epsilon$ , the maximum error allowed in the utility of any state
  local variables:  $U, U'$ , vectors of utilities for states in  $S$ , initially zero
                   $\delta$ , the maximum change in the utility of any state in an iteration

  repeat
     $U \leftarrow U'$ ;  $\delta \leftarrow 0$ 
    for each state  $s$  in  $S$  do
       $U'[s] \leftarrow R(s) + \gamma \max_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s']$ 
      if  $|U'[s] - U[s]| > \delta$  then  $\delta \leftarrow |U'[s] - U[s]|$ 
    until  $\delta < \epsilon(1 - \gamma)/\gamma$ 
  return  $U$ 
```

Figure 17.4 The value iteration algorithm for calculating utilities of states. The termination condition is from Equation (??).

```

function POLICY-ITERATION(mdp) returns a policy
  inputs: mdp, an MDP with states S, actions A(s), transition model  $P(s' | s, a)$ 
  local variables: U, a vector of utilities for states in S, initially zero
     $\pi$ , a policy vector indexed by state, initially random

  repeat
    U  $\leftarrow$  POLICY-EVALUATION( $\pi$ , U, mdp)
    unchanged?  $\leftarrow$  true
    for each state s in S do
      if  $\max_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s'] > \sum_{s'} P(s' | s, \pi[s]) U[s']$  then do
         $\pi[s] \leftarrow \operatorname{argmax}_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s']$ 
        unchanged?  $\leftarrow$  false
    until unchanged?
    return  $\pi$ 

```

Figure 17.7 The policy iteration algorithm for calculating an optimal policy.

```

function POMDP-VALUE-ITERATION(pomdp,  $\epsilon$ ) returns a utility function
  inputs: pomdp, a POMDP with states S, actions A(s), transition model  $P(s' | s, a)$ ,
    sensor model  $P(e | s)$ , rewards  $R(s)$ , discount  $\gamma$ 
     $\epsilon$ , the maximum error allowed in the utility of any state
  local variables: U, U', sets of plans p with associated utility vectors  $\alpha_p$ 

  U'  $\leftarrow$  a set containing just the empty plan [], with  $\alpha_{[]}(\cdot) = R(\cdot)$ 
  repeat
    U  $\leftarrow U'
    U'  $\leftarrow$  the set of all plans consisting of an action and, for each possible next percept,
      a plan in U with utility vectors computed according to Equation (??)
    U'  $\leftarrow$  REMOVE-DOMINATED-PLANS(U')
  until MAX-DIFFERENCE(U, U')  $< \epsilon(1 - \gamma)/\gamma$ 
  return U$ 
```

Figure 17.9 A high-level sketch of the value iteration algorithm for POMDPs. The REMOVE-DOMINATED-PLANS step and MAX-DIFFERENCE test are typically implemented as linear programs.

18 LEARNING FROM EXAMPLES

```
function DECISION-TREE-LEARNING(examples, attributes, parent-examples) returns a tree
  if examples is empty then return PLURALITY-VALUE(parent-examples)
  else if all examples have the same classification then return the classification
  else if attributes is empty then return PLURALITY-VALUE(examples)
  else
     $A \leftarrow \operatorname{argmax}_{a \in \text{attributes}} \text{IMPORTANCE}(a, \text{examples})$ 
    tree  $\leftarrow$  a new decision tree with root test A
    for each value  $v_k$  of A do
       $exs \leftarrow \{e : e \in \text{examples} \text{ and } e.A = v_k\}$ 
      subtree  $\leftarrow$  DECISION-TREE-LEARNING(exs, attributes - A, examples)
      add a branch to tree with label (A =  $v_k$ ) and subtree subtree
  return tree
```

Figure 18.4 The decision-tree learning algorithm. The function IMPORTANCE is described in Section ???. The function PLURALITY-VALUE selects the most common output value among a set of examples, breaking ties randomly.

```

function CROSS-VALIDATION-WRAPPER(Learner, k, examples) returns a hypothesis
  local variables: errT, an array, indexed by size, storing training-set error rates
    errV, an array, indexed by size, storing validation-set error rates
  for size = 1 to  $\infty$  do
    errT[size], errV[size]  $\leftarrow$  CROSS-VALIDATION(Learner, size, k, examples)
    if errT has converged then do
      best_size  $\leftarrow$  the value of size with minimum errV[size]
    return Learner(best_size, examples)

function CROSS-VALIDATION(Learner, size, k, examples) returns two values:
  average training set error rate, average validation set error rate
  fold_errT  $\leftarrow$  0; fold_errV  $\leftarrow$  0
  for fold = 1 to k do
    training_set, validation_set  $\leftarrow$  PARTITION(examples, fold, k)
    h  $\leftarrow$  Learner(size, training_set)
    fold_errT  $\leftarrow$  fold_errT + ERROR-RATE(h, training_set)
    fold_errV  $\leftarrow$  fold_errV + ERROR-RATE(h, validation_set)
  return fold_errT/k, fold_errV/k

```

Figure 18.7 An algorithm to select the model that has the lowest error rate on validation data by building models of increasing complexity, and choosing the one with best empirical error rate on validation data. Here *errT* means error rate on the training data, and *errV* means error rate on the validation data. *Learner*(*size*, *examples*) returns a hypothesis whose complexity is set by the parameter *size*, and which is trained on the *examples*. PARTITION(*examples*, *fold*, *k*) splits *examples* into two subsets: a validation set of size N/k and a training set with all the other examples. The split is different for each value of *fold*.

```

function DECISION-LIST-LEARNING(examples) returns a decision list, or failure
  if examples is empty then return the trivial decision list No
  t  $\leftarrow$  a test that matches a nonempty subset examplest of examples
    such that the members of examplest are all positive or all negative
  if there is no such t then return failure
  if the examples in examplest are positive then o  $\leftarrow$  Yes else o  $\leftarrow$  No
  return a decision list with initial test t and outcome o and remaining tests given by
    DECISION-LIST-LEARNING(examples  $-$  examplest)

```

Figure 18.10 An algorithm for learning decision lists.

```

function BACK-PROP-LEARNING(examples, network) returns a neural network
  inputs: examples, a set of examples, each with input vector  $\mathbf{x}$  and output vector  $\mathbf{y}$ 
          network, a multilayer network with  $L$  layers, weights  $w_{i,j}$ , activation function  $g$ 
  local variables:  $\Delta$ , a vector of errors, indexed by network node

  repeat
    for each weight  $w_{i,j}$  in network do
       $w_{i,j} \leftarrow$  a small random number
    for each example  $(\mathbf{x}, \mathbf{y})$  in examples do
      /* Propagate the inputs forward to compute the outputs */
      for each node  $i$  in the input layer do
         $a_i \leftarrow x_i$ 
      for  $\ell = 2$  to  $L$  do
        for each node  $j$  in layer  $\ell$  do
           $in_j \leftarrow \sum_i w_{i,j} a_i$ 
           $a_j \leftarrow g(in_j)$ 
      /* Propagate deltas backward from output layer to input layer */
      for each node  $j$  in the output layer do
         $\Delta[j] \leftarrow g'(in_j) \times (y_j - a_j)$ 
      for  $\ell = L - 1$  to 1 do
        for each node  $i$  in layer  $\ell$  do
           $\Delta[i] \leftarrow g'(in_i) \sum_j w_{i,j} \Delta[j]$ 
      /* Update every weight in network using deltas */
      for each weight  $w_{i,j}$  in network do
         $w_{i,j} \leftarrow w_{i,j} + \alpha \times a_i \times \Delta[j]$ 
    until some stopping criterion is satisfied
    return network
  
```

Figure 18.23 The back-propagation algorithm for learning in multilayer networks.

```

function ADABOOST(examples, L, K) returns a weighted-majority hypothesis
  inputs: examples, set of N labeled examples  $(x_1, y_1), \dots, (x_N, y_N)$ 
          L, a learning algorithm
          K, the number of hypotheses in the ensemble
  local variables: w, a vector of N example weights, initially  $1/N$ 
                    h, a vector of K hypotheses
                    z, a vector of K hypothesis weights

  for k = 1 to K do
    h[k]  $\leftarrow L(\text{examples}, \mathbf{w})$ 
    error  $\leftarrow 0$ 
    for j = 1 to N do
      if h[k](xj)  $\neq y_j$  then error  $\leftarrow error + w[j]$ 
    for j = 1 to N do
      if h[k](xj) = yj then w[j]  $\leftarrow w[j] \cdot error / (1 - error)$ 
    w  $\leftarrow \text{NORMALIZE}(\mathbf{w})$ 
    z[k]  $\leftarrow \log(1 - error) / error$ 
  return WEIGHTED-MAJORITY(h, z)

```

Figure 18.33 The ADABOOST variant of the boosting method for ensemble learning. The algorithm generates hypotheses by successively reweighting the training examples. The function WEIGHTED-MAJORITY generates a hypothesis that returns the output value with the highest vote from the hypotheses in **h**, with votes weighted by **z**.

19 KNOWLEDGE IN LEARNING

```
function CURRENT-BEST-LEARNING(examples, h) returns a hypothesis or fail
    if examples is empty then
        return h
    e  $\leftarrow$  FIRST(examples)
    if e is consistent with h then
        return CURRENT-BEST-LEARNING(REST(examples), h)
    else if e is a false positive for h then
        for each h' in specializations of h consistent with examples seen so far do
            h''  $\leftarrow$  CURRENT-BEST-LEARNING(REST(examples), h')
            if h''  $\neq$  fail then return h''
        else if e is a false negative for h then
            for each h' in generalizations of h consistent with examples seen so far do
                h''  $\leftarrow$  CURRENT-BEST-LEARNING(REST(examples), h')
                if h''  $\neq$  fail then return h''
    return fail
```

Figure 19.2 The current-best-hypothesis learning algorithm. It searches for a consistent hypothesis that fits all the examples and backtracks when no consistent specialization/generalization can be found. To start the algorithm, any hypothesis can be passed in; it will be specialized or generalized as needed.

```

function VERSION-SPACE-LEARNING(examples) returns a version space
  local variables:  $V$ , the version space: the set of all hypotheses

     $V \leftarrow$  the set of all hypotheses
    for each example  $e$  in examples do
      if  $V$  is not empty then  $V \leftarrow$  VERSION-SPACE-UPDATE( $V, e$ )
    return  $V$ 

function VERSION-SPACE-UPDATE( $V, e$ ) returns an updated version space
   $V \leftarrow \{h \in V : h \text{ is consistent with } e\}$ 

```

Figure 19.3 The version space learning algorithm. It finds a subset of V that is consistent with all the *examples*.

```

function MINIMAL-CONSISTENT-DET( $E, A$ ) returns a set of attributes
  inputs:  $E$ , a set of examples
     $A$ , a set of attributes, of size  $n$ 

  for  $i = 0$  to  $n$  do
    for each subset  $A_i$  of  $A$  of size  $i$  do
      if CONSISTENT-DET?( $A_i, E$ ) then return  $A_i$ 

function CONSISTENT-DET?( $A, E$ ) returns a truth value
  inputs:  $A$ , a set of attributes
     $E$ , a set of examples
  local variables:  $H$ , a hash table

  for each example  $e$  in  $E$  do
    if some example in  $H$  has the same values as  $e$  for the attributes  $A$ 
      but a different classification then return false
    store the class of  $e$  in  $H$ , indexed by the values for attributes  $A$  of the example  $e$ 
  return true

```

Figure 19.8 An algorithm for finding a minimal consistent determination.

```

function FOIL(examples, target) returns a set of Horn clauses
  inputs: examples, set of examples
           target, a literal for the goal predicate
  local variables: clauses, set of clauses, initially empty

  while examples contains positive examples do
    clause  $\leftarrow$  NEW-CLAUSE(examples, target)
    remove positive examples covered by clause from examples
    add clause to clauses
  return clauses

function NEW-CLAUSE(examples, target) returns a Horn clause
  local variables: clause, a clause with target as head and an empty body
                  l, a literal to be added to the clause
                  extended-examples, a set of examples with values for new variables

  extended-examples  $\leftarrow$  examples
  while extended-examples contains negative examples do
    l  $\leftarrow$  CHOOSE-LITERAL(NEW-LITERALS(clause), extended-examples)
    append l to the body of clause
    extended-examples  $\leftarrow$  set of examples created by applying EXTEND-EXAMPLE
      to each example in extended-examples
  return clause

function EXTEND-EXAMPLE(example, literal) returns a set of examples
  if example satisfies literal
    then return the set of examples created by extending example with
      each possible constant value for each new variable in literal
  else return the empty set

```

Figure 19.12 Sketch of the FOIL algorithm for learning sets of first-order Horn clauses from examples. NEW-LITERALS and CHOOSE-LITERAL are explained in the text.

20 LEARNING PROBABILISTIC MODELS

21 REINFORCEMENT LEARNING

```
function PASSIVE-ADP-AGENT(percept) returns an action
    inputs: percept, a percept indicating the current state  $s'$  and reward signal  $r'$ 
    persistent:  $\pi$ , a fixed policy
         $mdp$ , an MDP with model  $P$ , rewards  $R$ , discount  $\gamma$ 
         $U$ , a table of utilities, initially empty
         $N_{sa}$ , a table of frequencies for state-action pairs, initially zero
         $N_{s'|sa}$ , a table of outcome frequencies given state-action pairs, initially zero
         $s, a$ , the previous state and action, initially null

    if  $s'$  is new then  $U[s'] \leftarrow r'; R[s'] \leftarrow r'$ 
    if  $s$  is not null then
        increment  $N_{sa}[s, a]$  and  $N_{s'|sa}[s', s, a]$ 
        for each  $t$  such that  $N_{s'|sa}[t, s, a]$  is nonzero do
             $P(t | s, a) \leftarrow N_{s'|sa}[t, s, a] / N_{sa}[s, a]$ 
         $U \leftarrow \text{POLICY-EVALUATION}(\pi, U, mdp)$ 
    if  $s'$ .TERMINAL? then  $s, a \leftarrow \text{null}$  else  $s, a \leftarrow s', \pi[s']$ 
    return  $a$ 
```

Figure 21.2 A passive reinforcement learning agent based on adaptive dynamic programming. The POLICY-EVALUATION function solves the fixed-policy Bellman equations, as described on page ??.

```

function PASSIVE-TD-AGENT(percept) returns an action
  inputs: percept, a percept indicating the current state  $s'$  and reward signal  $r'$ 
  persistent:  $\pi$ , a fixed policy
     $U$ , a table of utilities, initially empty
     $N_s$ , a table of frequencies for states, initially zero
     $s, a, r$ , the previous state, action, and reward, initially null

  if  $s'$  is new then  $U[s'] \leftarrow r'$ 
  if  $s$  is not null then
    increment  $N_s[s]$ 
     $U[s] \leftarrow U[s] + \alpha(N_s[s])(r + \gamma U[s'] - U[s])$ 
  if  $s'.\text{TERMINAL?}$  then  $s, a, r \leftarrow \text{null}$  else  $s, a, r \leftarrow s', \pi[s'], r'$ 
  return  $a$ 

```

Figure 21.4 A passive reinforcement learning agent that learns utility estimates using temporal differences. The step-size function $\alpha(n)$ is chosen to ensure convergence, as described in the text.

```

function Q-LEARNING-AGENT(percept) returns an action
  inputs: percept, a percept indicating the current state  $s'$  and reward signal  $r'$ 
  persistent:  $Q$ , a table of action values indexed by state and action, initially zero
     $N_{sa}$ , a table of frequencies for state-action pairs, initially zero
     $s, a, r$ , the previous state, action, and reward, initially null

  if TERMINAL?( $s$ ) then  $Q[s, \text{None}] \leftarrow r'$ 
  if  $s$  is not null then
    increment  $N_{sa}[s, a]$ 
     $Q[s, a] \leftarrow Q[s, a] + \alpha(N_{sa}[s, a])(r + \gamma \max_{a'} Q[s', a'] - Q[s, a])$ 
     $s, a, r \leftarrow s', \text{argmax}_{a'} f(Q[s', a'], N_{sa}[s', a']), r'$ 
  return  $a$ 

```

Figure 21.8 An exploratory Q-learning agent. It is an active learner that learns the value $Q(s, a)$ of each action in each situation. It uses the same exploration function f as the exploratory ADP agent, but avoids having to learn the transition model because the Q-value of a state can be related directly to those of its neighbors.

22 NATURAL LANGUAGE PROCESSING

```
function HITS(query) returns pages with hub and authority numbers
  pages  $\leftarrow$  EXPAND-PAGES(RELEVANT-PAGES(query))
  for each p in pages do
    p.AUTHORITY  $\leftarrow$  1
    p.HUB  $\leftarrow$  1
  repeat until convergence do
    for each p in pages do
      p.AUTHORITY  $\leftarrow \sum_i \text{INLINK}_i(p).\text{HUB}$ 
      p.HUB  $\leftarrow \sum_i \text{OUTLINK}_i(p).\text{AUTHORITY}$ 
    NORMALIZE(pages)
  return pages
```

Figure 22.1 The HITS algorithm for computing hubs and authorities with respect to a query. RELEVANT-PAGES fetches the pages that match the query, and EXPAND-PAGES adds in every page that links to or is linked from one of the relevant pages. NORMALIZE divides each page's score by the sum of the squares of all pages' scores (separately for both the authority and hubs scores).

23 NATURAL LANGUAGE FOR COMMUNICATION

```
function CYK-PARSE(words, grammar) returns P, a table of probabilities
  N  $\leftarrow$  LENGTH(words)
  M  $\leftarrow$  the number of nonterminal symbols in grammar
  P  $\leftarrow$  an array of size [M, N, N], initially all 0
  /* Insert lexical rules for each word */
  for i = 1 to N do
    for each rule of form (X  $\rightarrow$  wordsi [p]) do
      P[X, i, 1]  $\leftarrow$  p
  /* Combine first and second parts of right-hand sides of rules, from short to long */
  for length = 2 to N do
    for start = 1 to N - length + 1 do
      for len1 = 1 to N - 1 do
        len2  $\leftarrow$  length - len1
        for each rule of the form (X  $\rightarrow$  YZ [p]) do
          P[X, start, length]  $\leftarrow$  MAX(P[X, start, length],
                                         P[Y, start, len1]  $\times$  P[Z, start + len1, len2]  $\times$  p)
  return P
```

Figure 23.4 The CYK algorithm for parsing. Given a sequence of words, it finds the most probable derivation for the whole sequence and for each subsequence. It returns the whole table, *P*, in which an entry *P*[*X*, *start*, *len*] is the probability of the most probable *X* of length *len* starting at position *start*. If there is no *X* of that size at that location, the probability is 0.

```
[ [S [NP-SBJ-2 Her eyes]
  [VP were
   [VP glazed
    [NP *-2]
    [SBAR-ADV as if
     [S [NP-SBJ she]
      [VP did n't
       [VP [VP hear [NP *-1]]
        or
        [VP [ADVP even] see [NP *-1]]
         [NP-1 him]]]]]]]
  .]
```

Figure 23.5 Annotated tree for the sentence “Her eyes were glazed as if she didn’t hear or even see him.” from the Penn Treebank. Note that in this grammar there is a distinction between an object noun phrase (*NP*) and a subject noun phrase (*NP-SBJ*). Note also a grammatical phenomenon we have not covered yet: the movement of a phrase from one part of the tree to another. This tree analyzes the phrase “hear or even see him” as consisting of two constituent *VPs*, [VP hear [NP *-1]] and [VP [ADVP even] see [NP *-1]], both of which have a missing object, denoted *-1, which refers to the *NP* labeled elsewhere in the tree as [NP-1 him].

24 PERCEPTION

25 ROBOTICS

```

function MONTE-CARLO-LOCALIZATION( $a, z, N, P(X'|X, v, \omega), P(z|z^*), m$ ) returns
a set of samples for the next time step
inputs:  $a$ , robot velocities  $v$  and  $\omega$ 
 $z$ , range scan  $z_1, \dots, z_M$ 
 $P(X'|X, v, \omega)$ , motion model
 $P(z|z^*)$ , range sensor noise model
 $m$ , 2D map of the environment
persistent:  $S$ , a vector of samples of size  $N$ 
local variables:  $W$ , a vector of weights of size  $N$ 
 $S'$ , a temporary vector of particles of size  $N$ 
 $W'$ , a vector of weights of size  $N$ 

if  $S$  is empty then /* initialization phase */
    for  $i = 1$  to  $N$  do
         $S[i] \leftarrow$  sample from  $P(X_0)$ 
    for  $i = 1$  to  $N$  do /* update cycle */
         $S'[i] \leftarrow$  sample from  $P(X'|X = S[i], v, \omega)$ 
         $W'[i] \leftarrow 1$ 
        for  $j = 1$  to  $M$  do
             $z^* \leftarrow \text{RAYCAST}(j, X = S'[i], m)$ 
             $W'[i] \leftarrow W'[i] \cdot P(z_j | z^*)$ 
     $S \leftarrow \text{WEIGHTED-SAMPLE-WITH-REPLACEMENT}(N, S', W')$ 
return  $S$ 

```

Figure 25.9 A Monte Carlo localization algorithm using a range-scan sensor model with independent noise.

26 PHILOSOPHICAL FOUNDATIONS

27

AI: THE PRESENT AND
FUTURE

28 MATHEMATICAL BACKGROUND

29

NOTES ON LANGUAGES AND ALGORITHMS

```
generator POWERS-OF-2() yields ints
    i ← 1
    while true do
        yield i
        i ← 2 × i
    -----
for p in POWERS-OF-2() do
    PRINT(p)
```

Figure 29.1 Example of a generator function and its invocation within a loop.